# Analysis and Design of $\mathbf{2 2 0} \mathbf{k V}$ Transmission Line Tower (A conventional method of analysis and Indian Code based Design) 

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#### Abstract

Transmission line tower constitute about 28 to 42 percent of the cost of the transmission power line project. The increasing demand for electricity can be made more economical by developing different light weight configuration of transmission line tower. In this study an attempt is made to model, analyse and design a $220 K V$ transmission line tower using manual calculations. The tower is designed in wind zone $-V$ with base width $1 / 5^{\text {th }}$ of total height of the tower. This objective is made by choosing a 220 KV single circuit transmission line carried by square base self-supporting tower with a view to optimize the existing geometry and then analysis of the tower has been carried out as a 2-D structure. Structure is made determinate by excluding the horizontal members and axial forces are calculated using method of joints and design is carried out as per IS 800:2007.


Keywords: Transmission towers, Geometry of tower, Self-supporting tower, Configuration oftower, unit load, method of joint, deflection, design.

## I. INTRODUCTION:

India has a large population residing all over the country and the electricity supply need of this population creates requirement of large transmission and distribution system. Also, the disposition of the primary resources for electrical power generation viz., coal, hydro potential is quite uneven, thus again adding to the transmission requirements. Transmission line is an integrated system consisting of conductor subsystem, ground wire subsystem and one subsystem for each category of support structure. Mechanical support of transmission line represents a significant portion of the cost of the line and they play an important role in the reliable power transmission. They are designed and constructed in wide variety of shapes, types, sizes, configuration and materials. The supporting structure types used in transmission line generally fall into one of the three categories: lattice, pole and guyed.

The supports of high voltage transmission lines are normally steel lattice towers. The cost of tower constitutes about quarter to half of the cost of transmission line and hence optimum tower design will bring in substantial savings. The selection of an optimum outline together with right type of bracing system contributes to a large extent in developing an economical design of transmission line tower. The height of tower is fixed by the user and the structural designer has the task of designing the general configuration and member and joint details. In this paper, the sag tension calculation is carried for conductor and ground wire using parabolic equation. Then different loading format including normal condition, top conductor broken, earth wire broken condition is evaluated.The wind loading is calculated on the longitudinal face of the towers and then two dimensional analysis of the tower is carried outand accordingly the design is completed for different members.

## II. Transmission Line Components:

### 2.1. Transmission Line Tower

The following parameters for transmission line and its components are assumed from I.S. 802: Part 1: Sec: 1:1995, I.S. 5613: Part 2: Sec: 1:1989.

- Transmission Line Voltage: 220 kV (A. / C.)
- Right of Way (recommended): 35, 000 mm
- Angle of Line Deviation: 0 to 2 degrees
- Terrain Type Considered: Plain
- No. of Circuits: Single Circuit
- Tower Configuration: Vertical Conductor Configuration
- Bracing Pattern: Pratt system
- Cross Arm: Pointed

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- Terrain Category: 2 (Normal cross country lines with very few obstacles)
- Return Period: 50 years
- Wind Zone: 5
- Basic Wind Speed: $50 \mathrm{~m} / \mathrm{s}$
- Design Wind Pressure: 793 N/sqm
- Tower Type: Self-Supporting, Type "A"
- Tower Geometry: Square Base Tower
- Inclination of the tower legs: 70 (with vertical)
- Shielding Angle: $30^{\circ}$
- Insulator Type: I String
- Number of Insulator Discs: 15
- Size of Insulator Disc: $255 \times 145 \mathrm{~mm}$ (Skirt Diameter)
- Length of Insulator String: 2,500 mm
- Creep Effect: Not Considered


### 2.2. Conductor

A substance or a material which allows the electric current to pass through its body when it is subjected to a difference of electric potential is known as Conductor. The properties of the conductor considered here are tabulated in Table1.

Table 1: Conductor mechanical and electrical properties.

| Conductor material | ACSR |
| :--- | :--- |
| Code name | Panther |
| Conductor size | $30 / 7 / 3.00 \mathrm{~mm}$ |
| Area of the conductor (for all strands), A | $2.6155 \mathrm{~cm}^{2}$ |
| Overall diameter of the conductor $(\mathrm{d})$ | 21 mm |
| Weight of the conductor $(\mathrm{w})$ | $0.973 \mathrm{~kg} / \mathrm{m}$ |
| Bearing strength of the conductor (UTS) | 9130 kg |
| Coefficient of linear expansion $(\alpha)$ | $17.73 \times 10^{-6} /{ }^{\circ} \mathrm{C}$ |
| Modulus of elasticity Final $\left(\mathrm{E}_{1}\right)$ | $0.787 \times 10^{6} \mathrm{kgf} / \mathrm{cm}^{2}$ |
| Modulus of elasticity Initial $\left(\mathrm{E}_{2}\right)$ | $0.626 \times 10^{6} \mathrm{kgf} / \mathrm{cm}^{2}$ |

### 2.3. Earthwire

The earthwire is used for protection against direct lightning strokes and the high voltage surges resulting there from. There will be one or two earthwire depending upon the shielding angle or protection angle. The earthwire considered for transmission line has the following properties as mentioned in Table 2.

Table 2: Earthwire mechanical and electrical properties

| Material of earthwire | Galvanized steel |
| :--- | :--- |
| No of earthwire | one |
| Stranding/wire diameter | $7 / 3.15 \mathrm{~mm}$ |
| Total sectional area | $54.55 \mathrm{~mm}^{2}$ |
| Overall diameter | 9.45 mm |
| Approximate weight | $428 \mathrm{~kg} / \mathrm{km}$ |
| Calculated D.C. resistance at $20^{\circ} \mathrm{C}$ | $3.375 \mathrm{ohm} / \mathrm{km}$ |
| Mini UTS | 5710 kg |
| Modulus of elasticity | $19361 \mathrm{~kg} / \mathrm{mm}^{2}$ |
| Coefficient of linear expansion | $11.50 \times 10^{-6} /{ }^{\circ} \mathrm{C}$ |
| Maximum allowable temperature | $53^{\circ} \mathrm{C}$ |

### 2.4. Insulator Strings

Insulators are devices used in the electrical system to support the conductors or to support the conductors carrying at given voltages. The insulators separate thecurrent carrying conductors of a transmission line from their support structures to prevent the flow of current through the structure to ground and to provide necessary mechanical support to the conductors at a safer height above the ground level.

## III. Sag tension for conductor and ground wire:

Indian standard codes of practice for use of structural steel in over-head transmission line towers have prescribed following conditions for the sagtension calculations for the conductor and the ground wire:

- Maximum temperature $\left(75^{\circ} \mathrm{C}\right.$ for ASCR and $53^{\circ} \mathrm{C}$ for ground wire) with design wind pressure $(0 \%$ and 36\%).
- Every day temperature $\left(32^{\circ} \mathrm{C}\right)$ and design wind pressure ( $100 \%, 75 \%$ and $0 \%$ ).
- Minimum temperature $\left(0^{\circ} \mathrm{C}\right)$ with design wind pressure ( $0 \%$ and $36 \%$ ).

IS 802: part 1:sec 1: 1995 states that conductor/ ground wire tension at every day temperature and without external load should not exceed $25 \%$ (up to 220 kV ) for conductors and $20 \%$ for ground wires oftheir ultimate tensile strength. Sag tensions are calculated by using the parabolic equations as discussed in the I.S. 5613: Part 2: Sec: 1: 1989 for both the conductor and ground wire. In this paper, the consideration of the sag of ground wire as $90 \%$ the sag of the conductor at $0^{\circ} \mathrm{C}$ and $100 \%$ wind condition. The sag tension values are mentioned in the Table 3.

### 3.1. Parabolic Equation

$F_{2}^{2}\left(\mathrm{~F}_{2}-(\mathrm{K}-\alpha . \mathrm{t} . \mathrm{E})\right)=\frac{\mathbb{L}^{2} \cdot a^{2} \cdot q_{2}^{2} E}{24}$
Take, $\mathrm{K}=\mathrm{F}_{1}-\frac{\mathbb{Z}^{2} \cdot a^{2} \cdot q q^{2} \cdot E}{24 F_{1}^{2}}$
Table 3. Sag tension for conductor (ASCR)

| Temperature variation ${ }^{\circ} \mathrm{C}$ | 0 |  |  | 32 | 75 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Wind variation $\%$ | 0 | 0.36 | 0 | 0.75 | 1.0 | 0 |
| Tension $(\mathrm{kg})$ | 2282.5 | 3733.0 | 3246.24 | 3108.30 | 3416.27 | 2367.23 |

All tension values are giving F.O.S < 4 .
So, we consider the minimum tension(tension for F.O.S = 4.) to find the maximum sagging in all condition.
So, sagging $=\frac{\mathrm{wl}^{2}}{8 T_{z}}=\frac{0.973 \times 320^{2}}{8 \times 2282.5}=5.46 \mathrm{~m}$
By increasing $4 \%$ of calculated sag we get $=5.46 \times 4 \%=5.70 \mathrm{~m}$.

## IV. Height of tower:

$\mathrm{h} 1=$ minimum permissible ground clearance $=7.1 \mathrm{~m}$ (cl=13.1,

IS:
5613.2.1)
$\mathrm{h} 2=\operatorname{sag}($ maximum $)=5.46 \times 1.04($ increase by $4 \%)=$ 5.7 m
$\mathrm{h} 3=$ minimum clearance between two conductor $=4.9 \mathrm{x}$ $2 \mathrm{~m} .=9.8 \mathrm{~m}(\mathrm{cl}=7.3 .1 .1$, IS: 5613.2.1)
$\mathrm{h} 4=$ vertical distance between earth and top conductor $=$ $7.4 \quad(\mathrm{cl}=13.2, \quad \mathrm{IS}: \quad 5613.2 .1)$

Total $\mathbf{H}=(\mathbf{h} \mathbf{1}+\mathbf{h} \mathbf{2}+\mathbf{h} \mathbf{3}+\mathbf{h} \mathbf{4})=30 \mathrm{~m}$
The dimension of the tower is shown in the Fig 1


Figure 1: Dimensions of tower in meter

## V. Wind loads on tower:

Wind loads on all the towers are calculated separately by developing excel programs by following Indian Standards. For finding the drag coefficients for the members of triangular tower, the solidity ratio is derived from Table 30 -IS-875 (part 3)-1987 in the similar fashion as prescribed in the IS- 826 (part-1/sec 1)1995.

### 5.1. Design Wind Pressure

To calculate design wind pressure on conductor, ground wire, insulator and panels: $\mathrm{P}_{\mathrm{d}}=0.6 \times \mathrm{V}_{\mathrm{d}}{ }^{2}$
Where, $\mathrm{P}_{\mathrm{d}}=$ design wind pressure in $\mathrm{N} / \mathrm{m}^{2}$
$\mathrm{V}_{\mathrm{d}}=$ design wind speed in $\mathrm{m} / \mathrm{s}$
To calculate design wind pressure, $\mathrm{V}_{\mathrm{d}}=\mathrm{V}_{\mathrm{R}} \times \mathrm{K}_{1} \times \mathrm{K}_{2}$ (4)
$\mathrm{V}_{\mathrm{R}}=10 \mathrm{~min}$ wind speed (or) reduced wind speed
$\mathrm{V}_{\mathrm{R}}=\mathrm{V}_{\mathrm{b}} / \mathrm{k}_{0}$
$\mathrm{V}_{\mathrm{b}}=$ basic wind speed
$\mathrm{K}_{0}=1.375$ [conversion factor]
$\mathrm{K}_{1}=$ risk coefficient
$\mathrm{K}_{2}=$ terrain roughness coefficient.

### 5.2. Wind Loads on Conductor/Ground Wire

To calculate wind loads on conductor and ground wire, $\mathrm{F}_{\mathrm{wc}}=\mathrm{P}_{\mathrm{d}} \times \mathrm{C}_{\mathrm{dc}} \times \mathrm{L} \times \mathrm{D} \times \mathrm{G}_{\mathrm{C}}$
Fwc $=$ wind load on conductor
$\mathrm{Pd}=$ design wind pressure
$\mathrm{Cdc}=$ drag coefficient for ground wire $=1.2$ drag coefficient for conductor $=1.0$
$\mathrm{L}=$ wind span
$\mathrm{d}=$ diameter of conductor/ground wire
$\mathrm{Gc}=$ gust response.

### 5.3. Wind Load on Insulator

To calculate wind load on insulator, $\mathrm{F}_{\mathrm{w}}=\mathrm{P}_{\mathrm{d}} \times \mathrm{C}_{\mathrm{di}} \times \mathrm{A}_{\mathrm{I}} \times \mathrm{G}_{\mathrm{I}}$
where, $\mathrm{A}_{\mathrm{I}}=50 \%$ area of insulator projected parallel to the longitudinal axis of string
$\mathrm{G}_{\mathrm{I}}=$ gust response factor for insulator
$\mathrm{C}_{\mathrm{di}}=$ drag coefficient, to be taken as 1.2150 mm

### 5.4.Wind Load on Panels

The lateral force due to wind acting at every panel joint is found as a product of intensity of wind and the exposed area of members of the tower consist of the projected area of the windward force plus fifty percent of plant of the leeward force. The sizes of the members taken are as

## Assuming-

Main leg: ISA $200 \times 200 \times 25$ single angle back to back section. For diagonal bracing: ISA $100 \times 100 \times 8$ single angle Horizontal bracing: ISA $130 \times 130 \times 10$ single angle Cross arm bracing: ISA $90 \times 90 \times 12$ single angle To calculate wind load on panels, $\mathbf{F}_{\mathbf{w}}=\mathbf{P}_{\mathrm{d}} \times \mathbf{C}_{\mathrm{dt}} \times \mathbf{A}_{\mathbf{e}} \times \mathbf{G}_{\mathbf{T}}$ $\mathrm{C}_{\mathrm{dt}}=$ drag coefficient for panel considered against which the wind is blowing
$\mathrm{A}_{\mathrm{e}} \quad=$ effective area of the panel
The wind load on panels for various conditions:

1. Normal operating conditions.
2. Top most power conductor in broken wire condition. 3. Ground wire in broken condition.

The Wind force acting at different panels are shown in Figure 2 and the


Figure 2: Wind Loads in Tower Panels

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values are tabulated in Table 4

Table 4. Lateral Force in Each Panel

| Lateral force | Under the various condition |  |  |
| :---: | :---: | :---: | :---: |
|  | Condition 1 (kN) | Condition 2 kN$)$ | Condition 3 kN$)$ |
| $\mathrm{P}_{\mathrm{L}}$ | 11.17 | 11.17 | 5.79 |
| $\mathrm{P}_{\mathrm{K}}$ | 3.965 | 3.965 | 3.965 |
| $\mathrm{P}_{\mathrm{J}}$ | 19.19 | 9.98 | 19.19 |
| $\mathrm{P}_{\mathrm{I}}$ | 3.89 | 3.89 | 3.89 |
| $\mathrm{P}_{\mathrm{H}}$ | 18.37 | 18.37 | 18.37 |
| $\mathrm{P}_{\mathrm{G}}$ | 3.72 | 3.72 | 3.72 |
| $\mathrm{P}_{\mathrm{F}}$ | 20.32 | 20.32 | 20.32 |
| $\mathrm{P}_{\mathrm{E}}$ | 4.47 | 4.47 | 4.47 |
| $\mathrm{P}_{\mathrm{D}}$ | 4.83 | 4.83 | 4.83 |
| $\mathrm{P}_{\mathrm{C}}$ | 5.21 | 5.21 | 5.21 |
| $\mathrm{P}_{\mathrm{B}}$ | 5.57 | 5.57 | 5.57 |

## VI. Stresses in the members of the tower under various conditions:

The transmission line tower as shown in the above figure is highly indeterminate. The stresses in the various members may be found by approximate method. The tower is reduced to a determinate plane frame by neglecting the horizontal and secondary members. The stresses are determined for the following conditions:

1. Normal operation conditions.
2. Due to lateral forces under the topmost power conductor broken condition.
3. Due to longitudinal forces under the topmost power conductor broken condition.
4. Due to lateral forces under the ground wire in broken condition.
5. Due to longitudinal forces under the ground wire in broken condition.

The axial forces in column and diagonal members are determined by the method of joints and by horizontal equilibrium and these values are shown in the table 5.

Table 5. Stresses in different members of the Tower

| Member | Conditions |  |  |
| :---: | :---: | :---: | :---: |
|  | Normal( kN ) | Top conductor broken (kN) | Earth wire broken (kN) |
| AB | 189.81 | 214.45 | 245.67 |
| $\mathrm{AB}^{\prime}$ | 11.83 | 23.10 | 10.29 |
| $\mathrm{A}^{\prime} \mathrm{B}^{\prime}$ | -189.81 | -214.45 | -245.67 |
| A'B | -11.83 | -23.10 | -10.29 |
| BC | 178.63 | 203.37 | 236.20 |
| BC' | 10.36 | 22.04 | 8.52 |
| $\mathrm{B}^{\prime} \mathrm{C}^{\prime}$ | -178.63 | -203.37 | -236.20 |
| B'C | -10.36 | -22.04 | -8.52 |
| CD | 167.63 | 192.53 | 227.56 |
| CD' | 9.18 | 21.45 | 6.88 |
| $\mathrm{C}^{\prime} \mathrm{D}^{\prime}$ | -167.63 | -192.53 | -227.56 |
| C'D | -9.18 | -21.45 | -6.88 |
| DE | 156.50 | 181.63 | 219.85 |
| DE' | 8.40 | 21.65 | 5.35 |
| $\mathrm{D}^{\prime} \mathrm{E}^{\prime}$ | -156.50 | -181.63 | -219.85 |
| D'E | -8.40 | -21.65 | -5.35 |
| EF | 144.55 | 170.04 | 213.35 |
| $\mathrm{EF}^{\prime}$ | 8.28 | 23.24 | 3.81 |
| $E^{\prime} \mathrm{F}^{\prime}$ | -144.55 | -170.04 | -213.35 |
| E'F | -8.28 | -23.24 | -3.81 |
| FG | 117.98 | 140.38 | 183.80 |


| Member | Conditions |  |  |
| :--- | :---: | :---: | :---: |
|  | Normal <br> $(\mathrm{kN})$ | Top <br> conductor <br> broken $(\mathrm{kN})$ | Earth wire <br> broken $(\mathrm{kN})$ |
| FG' $^{\text {F'G' }}$ | 26.33 | 45.27 | 34.32 |
| F'G | -117.98 | -140.38 | -183.80 |
| GH | -26.33 | -45.27 | -34.32 |
| GH' | 80.75 | 96.78 | 134.65 |
| G'H' | 24.14 | 43.51 | 32.31 |
| G'H | -80.75 | -96.78 | -134.65 |
| HI | -24.14 | -43.51 | -32.31 |
| HI' | 50.43 | 60.10 | 92.40 |
| H'I' | 16.88 | 35.82 | 24.87 |
| H'I | -50.43 | -60.10 | -92.40 |
| IJ | -16.88 | -35.82 | -24.87 |
| IJ' | 27.41 | 30.70 | 57.45 |
| I'J' | 14.34 | 33.71 | 22.52 |
| I'J' | -27.41 | -30.70 | -57.45 |
| JK | -14.34 | -33.71 | -22.52 |
| JK' | 11.61 | 11.65 | 29.73 |
| J'K' | 7.00 | 7.00 | 14.99 |
| J'K | -11.61 | -11.65 | -29.73 |
| KL | -7.00 | -7.00 | -14.99 |
| K'L | 7.12 | 7.16 | 20.57 |

Note: The positive value shown indicates tension and the negative value shown indicates compression for the various members of the tower and greater value under different conditions are highlighted.

## VII. Deflection of the members of the tower:

To determine the vertical deflection at joint B , first removed the externally applied load system and then applied a unit load only in a vertical direction at joint B as shown in Figure 3. After that the method of joint resolution is used as earlier to determine the magnitude and the unknown member forces. Similarly, the horizontal deflection at B can be determined by applying a unit load at B in the horizontal direction. The horizontal and vertical deflection is calculated under all three conditions as mentioned above for the entire panel joints (i.e. at joints B', C, C’, D, D', E, E', F, F', G, G', H, H', I, I', J, J', K, $\left.\mathrm{K}^{\prime}, \mathrm{L}\right)$ and tabulated in as shown in Table 6.


Figure 3: Unit load apply at panel jointB.

Table 6: Deflection at all panel joints

| Panel Joint | Maximum Deflection |  |
| :--- | :---: | :---: |
|  | Horizontal | Vertical |
| B | 0.682 | -0.346 |
| $\mathrm{~B}^{\prime}$ | 0.682 | 0.346 |
| $\mathrm{C}^{\prime}$ | 1.621 | -0.632 |
| $\mathrm{C}^{\prime}$ | 1.621 | 0.632 |
| D | 2.882 | -0.851 |
| $\mathrm{D}^{\prime}$ | 2.882 | 0.851 |
| E | 4.533 | -0.992 |
| $\mathrm{E}^{\prime}$ | 4.533 | 0.992 |
| F | 6.685 | -1.041 |
| $\mathrm{~F}^{\prime}$ | 6.685 | 1.041 |
| G | 9.652 | -1.276 |


| Panel Joint | Maximum Deflection |  |
| :--- | :---: | :---: |
|  | Horizontal | Vertical |
| $\mathrm{G}^{\prime}$ | 9.652 | 1.276 |
| $\mathrm{H}^{\prime}$ | 13.236 | -1.456 |
| $\mathrm{H}^{\prime}$ | 13.236 | 1.456 |
| I | 16.874 | -1.574 |
| $\mathrm{I}^{\prime}$ | 16.874 | 1.574 |
| J | 20.846 | -1.651 |
| $\mathrm{~J}^{\prime}$ | 20.846 | 1.651 |
| K | 24.661 | -1.689 |
| $\mathrm{~K}^{\prime}$ | 24.661 | 1.689 |
| L | 28.508 | 0 |
|  |  |  |

## VIII. Design of the members of the tower:

In X-type bracings the member which is under tension, due to lateral load acting in one direction, undergoes compressive force, when the direction of the lateral load is changed and vice-versa (as in the member force calculations).
Hence, such members are to be designed to resist both tensile and compressive forces.
The Members used in the Towers are standard Indian Angles of:

1. Main leg: ISA $200 \times 200 \times 25$ single angle back to back section.
2. Diagonal and Cross arm bracing: ISA $100 \times 100 \times 8$ single angle.
3. Horizontal bracing: ISA $130 \times 130 \times 10$ single angle.

The gusset plate is of 20 mm thickness and connection of gusset plate with angles is shown in Figure 4.


Figure 2: Angles Eccentrically Loaded through Gussets

### 7.1 Design of tension member by limit state method (IS 800:2007)

Tension members are linear members in which axial forces act to cause elongation (stretch). Such members can sustain loads up to the ultimate load, at which stage they may fail by rupture at a critical section. The design strength of the tension member shall be minimum of $\mathrm{T}_{\mathrm{dg}}, \mathrm{T}_{\mathrm{dn}}$ and $\mathrm{T}_{\mathrm{db}}$.
7.1.1 Strength Due To Yielding of Gross Section

The design strength in the member under axial tension is given by:
$\mathrm{T}_{\mathrm{dg}}=\mathrm{f}_{\mathrm{y}} \mathrm{A}_{\mathrm{g}} / \gamma_{\mathrm{mo}}$, where
$\gamma_{\mathrm{mo}}=$ the partial safety factor for failure in tension by yielding. The value of $\gamma_{\mathrm{mo}}$ according to IS800:2007 is 1.10.
7.1.2 Design Strength Due To Rupture of Critical Section

Tension rupture of the plate at the net cross-section is given by:
$\mathrm{T}_{\mathrm{dn}}=0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{n}} / \gamma_{\mathrm{ml}}$, where
$\gamma_{\mathrm{ml}}=$ the partial safety factor against ultimate tension failure by rupture $\left(\gamma_{\mathrm{ml}}=1.25\right)$
Single Angle Tension Member:
The strength of an angle connected by one leg as governed by tearing at the net section is given by,
$\mathrm{T}_{\mathrm{dn}}=0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{nc}} / \gamma_{\mathrm{ml}}+\beta \mathrm{A}_{\mathrm{go}} \mathrm{f}_{\mathrm{y}} / \gamma_{\mathrm{m} 0}$, where
$\beta$ accounts for the end fastener restraint effect and is given by
$\beta=1.4-0.076(w / t)\left(f_{u} / f_{y}\right)\left(b_{s} / L_{c}\right) \leq\left(f_{u} \gamma_{m 0} / f_{y} \gamma_{m 1}\right) \geq 0.7$
The $b_{s}$ (shear lag distance) is calculatedas shown in the Figure 5


Figữe 3: Añgles with Eñd Connection.

### 7.1.3Design Strength Due To Block Shear

A tension member may fail along end connection due to block shear as shown in Figure 6. The corresponding design strength can be evaluated using the following equations. The block shear strength $\mathrm{T}_{\mathrm{db}}$, at an end connection is taken as the smaller of


Figure 4: Block Shear Failure.

### 7.2Design charts tension member

The charts have been prepared based on IS 800:2007 for Tension members. The procedure is shown below.
Assumed material properties:
$\mathrm{f}_{\mathrm{y}}=250 \mathrm{MPa}, \mathrm{f}_{\mathrm{u}}=400 \mathrm{MPa}, \mathrm{f}_{\mathrm{ub}}=410 \mathrm{MPa}$

### 7.2.1 Design chart for Main leg ISA $200 \times 200 \times 25$

Tensile Strength of Single Angle ISA 200 X 200 X 25 (As per IS 800:2007) with single row bolted connection as shown in Figure 7 ( 9 nos. 20mm dia.).

The no of bolts considered for the design of tension members for end connections is based on minimum no. of bolts required for the full strength of the angle for Block shear.


Figure 7: Design Details of leg member (All Dimensions are in mm).
Design strength due to yielding of gross section
$\mathrm{T}_{\mathrm{dg}}=\mathrm{f}_{\mathrm{y}} \mathrm{A}_{\mathrm{g}} / \gamma_{\mathrm{mo}}$
$\mathrm{A}_{\mathrm{g}}=9380 \mathrm{~mm}^{2}$ (from steel table), $\gamma_{\mathrm{m} 0}=1.1$
$\mathrm{T}_{\mathrm{dg}}=250 \times 9380 / 1.1=2131.818 \mathrm{kN}$

### 7.2.1.1 Design Strength due to rupture of critical section

$\mathrm{e}=40 \mathrm{~mm}, \mathrm{p}=60 \mathrm{~mm}$
$\mathrm{T}_{\mathrm{dn}}=0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{nc}} / \gamma_{\mathrm{ml}}+\beta \mathrm{A}_{\mathrm{go}} \mathrm{f}_{\mathrm{y}} / \gamma_{\mathrm{m} 0}$
$\mathrm{A}_{\mathrm{nc}}=(200-22-25 / 2) \times 25=4137.5 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{go}}=(200-25 / 2) \times 25=4687.5 \mathrm{~mm}^{2}$
$\beta=1.4-0.076(w / t)\left(\mathrm{f}_{\mathrm{u}} / \mathrm{f}_{\mathrm{y}}\right)\left(\mathrm{b}_{\mathrm{s}} / \mathrm{L}_{\mathrm{c}}\right) \leq\left(\mathrm{f}_{\mathrm{u}} \gamma_{\mathrm{m} 0} / \mathrm{f}_{\mathrm{y}} \gamma_{\mathrm{m} 1}\right) \geq 0.7$
$\mathrm{L}_{\mathrm{c}}=60 \times 8=480, \mathrm{~b}_{\mathrm{s}}=200+140-25=315$
$\beta=1.4-0.076(200 / 25)(250 / 410)((315) / 480)=1.156(>0.7)$
$1.156<\left(\mathrm{f}_{\mathrm{u}} \gamma_{\mathrm{m} 0} / \mathrm{f}_{\mathrm{y}} \gamma_{\mathrm{m} 1}\right)=(410 \times 1.1) /(250 \times 1.25)=1.44$
Therefore, $\mathrm{T}_{\mathrm{dn}}=(0.9 \times 4137.5 \times 410) / 1.25+(1.15 \times 4687.5 \times 250) / 1.1=2446.5 \mathrm{kN}$

### 7.2.1.2 Design strength due to block shear

The block shear strength $T_{d b}$, at an end connection is taken as the smaller of
$\mathrm{T}_{\mathrm{db} 1}=\left(\mathrm{A}_{\mathrm{vg}} \mathrm{f}_{\mathrm{y}} /\left(\sqrt{ } 3 \gamma_{\mathrm{m} 0}\right)+0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{tr}} / \gamma_{\mathrm{m} 1}\right)$ or, $\mathrm{T}_{\mathrm{db} 2}=\left(0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{vn}} /\left(\sqrt{ } 3 \gamma_{\mathrm{m} 1}\right)+\mathrm{f}_{\mathrm{y}} \mathrm{A}_{\mathrm{tg}} / \gamma_{\mathrm{m} 0}\right)$
$\mathrm{A}_{\mathrm{vg}}=(40+60 \times 8) \times 25=13000 \mathrm{~mm}^{2}$
$A_{v n}=(40+60 \times 8-22 \times 7.5) \times 25=8325 \mathrm{~mm}^{2}$
$A_{t g}=(60 \times 25)=1500 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{tn}}=(60-0.5 \times 22) \times 25=1225 \mathrm{~mm}^{2}$
$\mathrm{T}_{\mathrm{db} 1}=((13000 \times 250) /(\sqrt{3} \times 1.1))+((0.9 \times 1225 \times 410) / 1.25)=2067 \mathrm{kN}$
Or, $\mathrm{T}_{\mathrm{db} 2}=((0.9 \times 8325 \times 410) /(\sqrt{3} \times 1.25))+((1500 \times 250) / 1.1)=1759 \mathrm{kN}$
Therefore, the block shear strength is $\mathrm{T}_{\mathrm{db}}=1759 \mathrm{kN}$
Now, Strength of the single angle Tension member should be least of the above three values (i.e. 2131.81 kN , 2446.5 kN and 1759 kN ) which is equal to 1759 kN .

As per our calculation we get that the maximum tension force is in the leg member of the ground panel which is 245.67 kN i.e. factored load $=245.67 \times 1.5=368.5 \mathrm{kN}$ is lesser than the above three values. Therefore our design is safe for maximum tension.

### 7.2.2 Design chart for Diagonal member ISA $100 \times 100 \times 8$

Tensile Strength of Single Angle ISA 100 X 100 X 8 (As per IS 800:2007) with single row bolted connection as shown in Figure 8 ( 3 nos 16 mm dia.).

The no of bolts considered for the design of tension members for end connections is based on minimum no. of bolts required for the full strength of the angle for Block shear.


Figure 8: Design Details of diagonal member (All dimensions are in mm).

### 7.2.2.1 Design strength due to yielding of gross section

$\mathrm{T}_{\mathrm{dg}}=\mathrm{f}_{\mathrm{y}} \mathrm{A}_{\mathrm{g}} / \gamma_{\mathrm{mo}}$
$\mathrm{A}_{\mathrm{g}}=1539 \mathrm{~mm}^{2}$ (from steel table), $\gamma_{\mathrm{m} 0}=1.1$
$\mathrm{T}_{\mathrm{dg}}=250 \times 1539 / 1.1=349.7 \mathrm{kN}$
7.2.2.2 Design Strength due to rupture of critical section
$\mathrm{e}=40 \mathrm{~mm}, \mathrm{p}=60 \mathrm{~mm}$
$\mathrm{T}_{\mathrm{dn}}=0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{nc}} / \gamma_{\mathrm{ml}}+\beta \mathrm{A}_{\mathrm{go}} \mathrm{f}_{\mathrm{y}} / \gamma_{\mathrm{m} 0}$
$A_{\mathrm{nc}}=(100-18-8 / 2) \times 8=624 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{go}}=(100-8 / 2) \times 8=768 \mathrm{~mm}^{2}$
$\beta=1.4-0.076(\mathrm{w} / \mathrm{t})\left(\mathrm{f}_{\mathrm{u}} / \mathrm{f}_{\mathrm{y}}\right)\left(\mathrm{b}_{\mathrm{s}} / \mathrm{L}_{\mathrm{c}}\right) \leq\left(\mathrm{f}_{\mathrm{u}} \gamma_{\mathrm{m} 0} / \mathrm{f}_{\mathrm{y}} \gamma_{\mathrm{m} 1}\right) \geq 0.7$
$\mathrm{L}_{\mathrm{c}}=60 \times 2=120, \mathrm{~b}_{\mathrm{s}}=100+44-8=136$
$\beta=1.4-0.076(100 / 8)(250 / 410)((136) / 480)=0.74(>0.7)$
$0.74<\left(\mathrm{f}_{\mathrm{u}} \gamma_{\mathrm{m} 0} / \mathrm{f}_{\mathrm{y}} \gamma_{\mathrm{m} 1}\right)=(410 \times 1.1) /(250 \times 1.25)=1.44$
Therefore, $\mathrm{T}_{\mathrm{dn}}=(0.9 \times 624 \times 410) / 1.25+(0.74 \times 768 \times 250) / 1.1=313 \mathrm{kN}$

### 7.2.2.3 Design strength due to block shear

The block shear strength $\mathrm{T}_{\mathrm{db}}$, at an end connection is taken as the smaller of
$\mathrm{T}_{\mathrm{db} 1}=\left(\mathrm{A}_{\mathrm{vg}} \mathrm{f}_{\mathrm{y}} /\left(\sqrt{ } 3 \gamma_{\mathrm{m} 0}\right)+0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{t}} / \gamma_{\mathrm{m} 1}\right) \quad$ or, $\mathrm{T}_{\mathrm{db} 2}=\left(0.9 \mathrm{f}_{\mathrm{u}} \mathrm{A}_{\mathrm{vn}} /\left(\sqrt{ } 3 \gamma_{\mathrm{m} 1}\right)+\mathrm{f}_{\mathrm{y}} \mathrm{A}_{\mathrm{tg}} / \gamma_{\mathrm{m} 0}\right)$
$A_{v g}=(40+60 \times 2) \times 8=1280 \mathrm{~mm}^{2}$
$A_{v n}=(40+60 \times 2-18 \times 2.5) \times 8=920 \mathrm{~mm}^{2}$
$A_{t g}=(40+18) \times 8=464 \mathrm{~mm}^{2}$
$\mathrm{A}_{\mathrm{tn}}=(40+18-0.5 \times 18) \times 8=392 \mathrm{~mm}^{2}$
$\mathrm{T}_{\mathrm{db} 1}=((1280 \times 250) /(\sqrt{3} \times 1.1))+((0.9 \times 392 \times 410) / 1.25)=283.6 \mathrm{kN}$
Or, $\mathrm{T}_{\mathrm{db} 2}=((0.9 \times 920 \times 410) /(\sqrt{3} \times 1.25))+((464 \times 250) / 1.1)=262 \mathrm{kN}$
Therefore, the block shear strength is $\mathrm{T}_{\mathrm{db}}=262 \mathrm{kN}$
Now, Strength of the single angle Tension member should be least of the above three values (i.e. 349.7 kN , 313 kN and 262 kN ) which is equal to 262 kN .

As per the calculation, the maximum tension force is obtained in the diagonal member of the sixth panel which is 45.27 kN i.e. factored load $=45.27 \times 1.5=67.9 \mathrm{kNis}$ lesser than the above three values. Therefore the design is safe for maximum tension.

### 7.3 Design of compression member by limit state method (IS 800:2007)

7.3.1.Design chart for Main leg ISA $200 \times 200 \times 25$

Length $=3.02 \mathrm{~m}$
$\mathrm{K}=0.85$
$\mathrm{f}_{\mathrm{y}}=250 \mathrm{MPa}$
$\mathrm{A}=9380 \mathrm{~mm}^{2}$
$\mathrm{r}_{\text {min }}=60.5 \mathrm{~mm}$
$\mathrm{KL} / \mathrm{r}_{\text {min }}=(0.85 \times 3020) / 60.5=42.43$
From Table 10 of IS 800:2007, the member belongs to buckling class c.
Therefore, from Table 9(c) of IS 800:2007 the values of $\mathrm{f}_{\mathrm{cd}}$ are found using KL/r $=42.43$ and $\mathrm{f}_{\mathrm{y}}=250 \mathrm{MPa}$.

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Here,
For, $\mathrm{KL} / \mathrm{r}=40 \Rightarrow \mathrm{f}_{\mathrm{cd}}=198 \mathrm{MPa}$
$\mathrm{KL} / \mathrm{r}=50 \Rightarrow \mathrm{f}_{\mathrm{cd}}=183 \mathrm{MPa}$
Therefore, for $\mathrm{KL} / \mathrm{r}=42.43$
$\mathrm{f}_{\mathrm{cd}}=194.35 \mathrm{~N} / \mathrm{mm}^{2}$
Thus, strength of the angle as column
$\mathrm{P}_{\mathrm{d}}=\mathrm{A} \times \mathrm{f}_{\mathrm{cd}}=9380 \times 194.35=1823050 \mathrm{~N}=1823 \mathrm{kN}$
Working load $=1823 / 1.5=1215 \mathrm{kN}>245.67 \mathrm{kN}$
Therefore, the section is safe for maximum compressive force.

## IX. CONCLUSIONS

The transmission line tower is a statically indeterminate structure and the manual analysis of such a structure is very complex. A rigorous analysis considering three dimensional space actions is quite difficult. The development and application of computer analysis opened up a new and practically unlimited possibilities for the exact solution of these statically indeterminate structures with precise statically analysis of their three dimensional performance. However the adopted method of analysis presented in this paper considering linear behavior with two dimensional approaches gives satisfactory results which should be further verified with advanced software like STAAD Pro, Ansys etc. As per the design concern all section we consider are found safe against worst condition. In summary, the study presented here would certainly useful for Design Engineers basically for the new learners for better understanding the behaviors and the method of analysis and design of the transmission tower as per Indian Standard Codes of practice in a very simple and easy manner.

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